

# **CONCURRENT SYSTEMS**

## **LECTURE 7**

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## MUTEX-free Concurrency

Critical sections (i.e., locks) have drawbacks:

- If not put at the right level of granularity, they unnecessarily reduce concurrency (and efficiency)
- Delays of one process may affect the whole system (limit case: crash during a CS)

**MUTEX-freedom:** the only atomicity is the one provided by the primitives themselves (no wrapping of code into CSs)

→ the liveness properties used so far cannot be used anymore, since they rely on CSs

1. **Obstruction freedom**: every time an operation is run in isolation (no overlap with any other operation on the same object), it terminates.
2. **Non-blocking**: whenever an operation is invoked on an object, eventually one operation on that object terminates  
→ reminds deadlock-freedom in MUTEX-based concurrency
3. **Wait freedom**: whenever an operation is invoked on an object, it eventually terminates  
→ reminds starvation-freedom in MUTEX-based concurrency
4. **Bounded wait freedom**: W.F. plus a bound on the number of steps needed to terminate  
→ reminds bounded bypass in MUTEX-based concurrency

**REMARK:** these notions naturally cope with (crash) failures → fail stop is another way of terminating  
→ there is no way of distinguishing a failure from an arbitrary long sleep (bec. of asynchrony)



## A wait-free Splitter

Assume to have atomic R/W registers.

A **splitter** is a concurrent object that provides a single operation *dir* such that:

1. (*validity*) it returns L, R or S (left, right, stop)
2. (*concurrency*) in case of  $n$  simultaneous invocations of *dir*
  - a. At most  $n-1$  L are returned
  - b. At most  $n-1$  R are returned
  - c. At most 1 S is returned
3. (*wait freedom*) it eventually terminates

Idea:

- Not all processes obtain the same value
- In a solo execution (i.e., without concurrency) the invoking process must stop (0 L && 0 R && at most 1 S)





## A wait-free Splitter

We have:

- DOOR : MRMW boolean atomic register initialized at 1
- LAST : MRMW atomic register initialized at whatever process index

```
dir(i) :=  
    LAST ← i  
    if DOOR = 0 then return R  
        else DOOR ← 0  
            if LAST = i then return S  
                else return L
```

With 2 processes, you can have

- One goes left and one goes right
- One goes left and the other stops
- One goes right and the other stops



*Proof:*

1. Not all proc's can obtain R

## 2. Not all proc's can obtain L

→ if the door is closed, it receives R and  $\checkmark$   
otherwise, it finds LAST=i and receives S →  $\checkmark$

→ it has written LAST before i → it doesn't find LAST=j in its  
second if and receives L →  $\sqrt{}$

→ it has written LAST after i → it finds the door closed and receives R →  $\checkmark$





# An Obstruction-free Timestamp Generator

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A **timestamp generator** is a concurrent object that provides a single operation `get_ts` such that:

1. (*validity*) not two invocations of `get_ts` return the same value
2. (*consistency*) if one process terminates its invocation of `get_ts` before another one starts, the first receives a timestamp that is smaller than the one received by the second one
3. (*obstruction freedom*) if run in isolation, it eventually terminates

Idea: use something like a splitter for possible timestamp, so that only the process that receives S (if any) can get that timestamp.





## An Obstruction-free Timestamp Generator

We have:

- DOOR[i] : MRMW boolean atomic register initialized at 1, for all i
- LAST[i] : MRMW atomic register initialized at whatever process index, for all i
- NEXT : integer initialized at 1

```
get_ts(i) :=  
    k ← NEXT  
    while true do  
        LAST[k] ← i  
        if DOOR[k] = 1 then  
            DOOR[k] ← 0  
            if LAST[k] = i then NEXT++  
            return k  
        k++
```



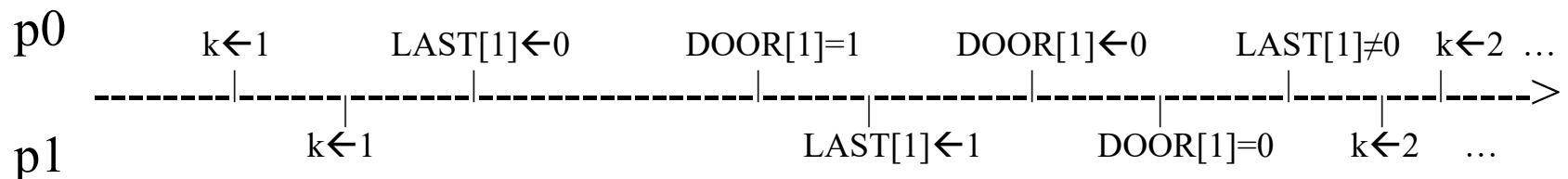


**Thm (soundness):** this implementation satisfies the 3 properties of the timestamp generator

*Proof:*

1. Validity holds because of property 2.c of the splitter
2. For consistency, the invocation that terminates increased the val of NEXT before terminating  
→ every process that starts after its termination will find NEXT to a greater value (NEXT never decreases!)
3. Obstruction freedom is trivial

REMARK: this implementation doesn't satisfy the non-blocking property:







## A Wait-free Stack

REG is an unbounded array of atomic registers (the stack)

For all  $i$ ,  $\text{REG}[i]$  can be

- Written
- Read by the  $\text{swap}(v)$  primitives (that atomically writes a new value in it)
- Initialized at  $\perp$

NEXT is an atomic register (pointing at the next free location of the stack) that can be

- Read
- Fetch&add
- Initialized at 1

```
push(v) :=  
    i ← NEXT.fetch&add(1)  
    REG[i] ← v
```

```
pop() :=  
    k ← NEXT-1  
    for i=k downto 1  
        tmp ← REG[i].swap( $\perp$ )  
        if tmp $\neq \perp$  then return tmp  
    return  $\perp$ 
```

REMARK: crashes do not compromise progress!

PROBLEM: unboundedness of REG is not realistic





## A Non-blocking Bounded Stack

Idea: every operation is started by the invoking process and finalized by the next process

STACK[0..k] : an array of registers that can be read or compare&setted

→ STACK[i] is actually a pair  $\langle \text{val}, \text{seq\_numb} \rangle$  initialized at  $\langle \perp, 0 \rangle$

This is needed for the so called ABA problem with compare&set:

- A typical use of compare&set is  $\text{tmp} \leftarrow X$   
...  
if  $X.\text{compare\&set}(\text{tmp}, v)$  then ...
- This is to ensure that the value of X has not changed in the computation
- The problem is that X can be changed twice before the comp&set
- Solution: X is a pair  $\langle \text{val}, \text{seq\_numb} \rangle$ , with the constraint that each modification of X increases its seq\_numb  
→ with the comp&set you mainly test that the seq\_numb has not changed

TOP : a register that can be read or compare&setted

→ TOP is actually a triple  $\langle \text{index}, \text{val}, \text{seq\_numb} \rangle$  initialized at  $\langle 0, \perp, 1 \rangle$

where the  
top is in STACK

the pair to be put  
at the top of STACK



## A Non-blocking Bounded Stack

```
push(w) :=  
  while true do  
     $\langle i, v, s \rangle \leftarrow \text{TOP}$   
    conclude(i, v, s)  
    if i=k then return FULL  
    newtop  $\leftarrow \langle i+1, w, \text{STACK}[i+1].\text{seq\_num}+1 \rangle$   
    if TOP.compare&set( $\langle i, v, s \rangle$ , newtop)  
    then return OK  
  
    conclude(i, v, s) :=  
      tmp  $\leftarrow \text{STACK}[i].\text{val}$   
      STACK[i].compare&set( $\langle \text{tmp}, s-1 \rangle, \langle v, s \rangle$ )  
  
pop() :=  
  while true do  
     $\langle i, v, s \rangle \leftarrow \text{TOP}$   
    conclude(i, v, s)  
    if i=0 then return EMPTY  
    newtop  $\leftarrow \langle i-1, \text{STACK}[i-1] \rangle$   
    if TOP.compare&set( $\langle i, v, s \rangle$ , newtop)  
    then return v
```



## A Non-blocking Bounded Stack

**Thm (liveness):** the implementation of the stack is non-blocking.

*Proof:*

Let us consider an operation invocation performed by p

- if it terminates  $\rightarrow \checkmark$
- otherwise, TOP has changed between the first of TOP and the last Compare&set
  - $\rightarrow$  the only instruction that modifies TOP is the closing Compare&set
  - $\rightarrow$  another operation invocation (issued by another process) has terminated  $\rightarrow \checkmark$

REMARK: the fact that the operation is concluded by the next process, together with atomicity of compare&set, ensures correctness even with crash failures

- $\rightarrow$  if it was part of the invocation (just before the final return of push/pop), a failure just after the TOP.compare&set would compromise consistency

